

# Quiz Section Week 5

## April 26, 2016

### Review

Programming: Matrices, files, more on  
functions, organizing programs

# Topics (not guaranteed to be comprehensive!)

- Alignments
  - Reasons to align sequences
  - Needleman-Wunsch algorithm
  - Smith-Waterman algorithm
  - Effects of parameter variation (including gap penalties)
  - Testing for statistical significance of an alignment
- Phylogenetic trees
  - Rooted and unrooted topologies
  - Defining the best tree with UPGMA and Neighbor Joining
  - Concept of parsimony
  - Fitch algorithm: quantifying how parsimonious a tree is, assigning internal states
  - Finding the most parsimonious tree: Hill climbing w/ Nearest-Neighbor interchanges
  - Bootstrapping to quantify confidence in tree partitions
- Clustering
  - Defining a clustering problem
  - Hierarchical clustering
    - Impact of using single/complete/average linkage
  - K-means: Objective and algorithm
- General computation and programming
  - What is an algorithm
  - What is a search heuristic
  - Conceptual definitions of variable and function
  - Algorithm complexity with  $O(n)$  notation
  - Data types and converting between them
  - Program flow and control with conditional statements and loops

# Phylogenetic trees

## **UPGMA/Neighbor Joining**

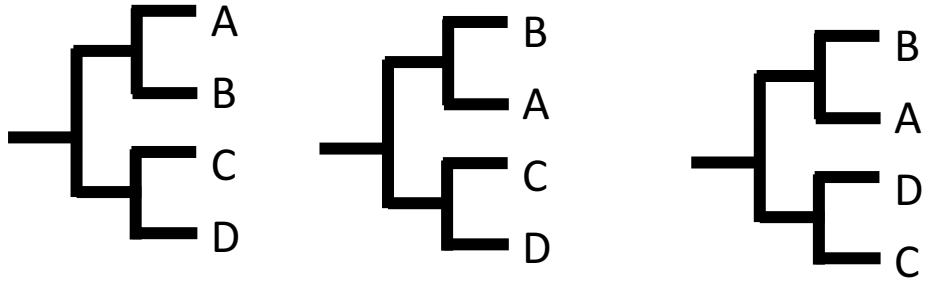
- Define the best tree: based on distance between leaves
- Find the best tree using: polynomial time algorithm to construct the best tree from a distance matrix

## **Parsimony approach**

- Define the best tree: Minimum # of mutations required to traverse tree
- Find the best tree: by enumerating all trees (exhaustive search), or by heuristic approach like Nearest-Neighbor Interchange Hill-Climbing

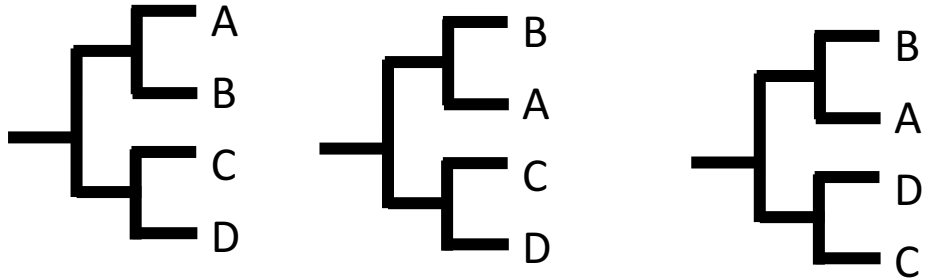
# Tree topologies

Are these the same tree?

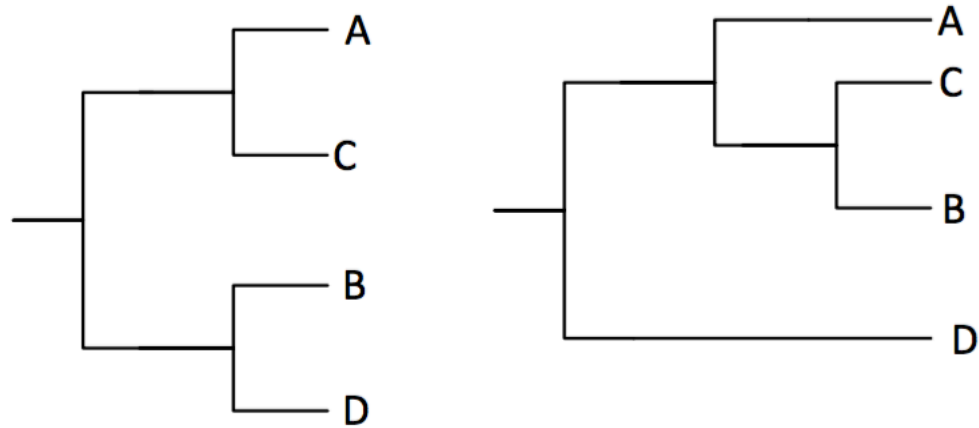


# Tree topologies

Are these the same tree?



How about these?



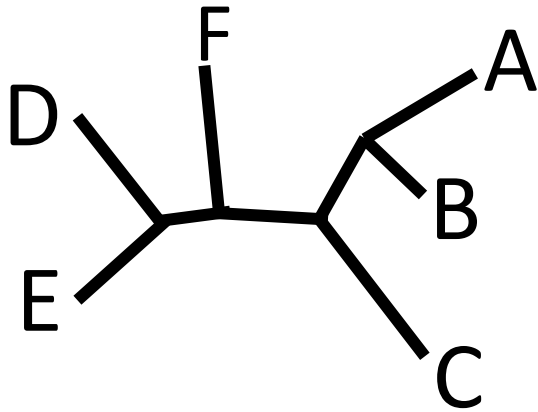
# Counting tree topologies

For N leaves

# of unrooted topologies =  $3 * 5 * 7 * \dots * (2N - 5)$

# of branches =  $2N - 3$

E.g. an unrooted tree with 6 nodes



How many different topologies?

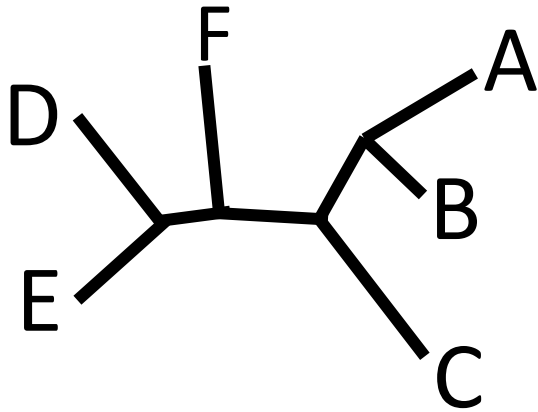
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How many different topologies?

$$3*5*7 = \mathbf{105}$$

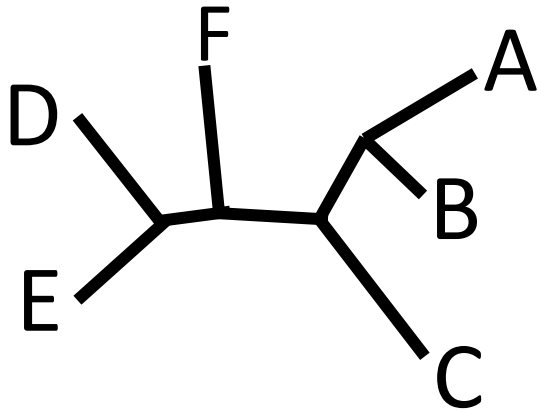
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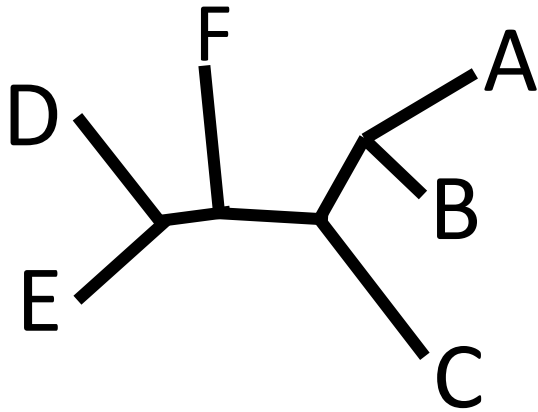
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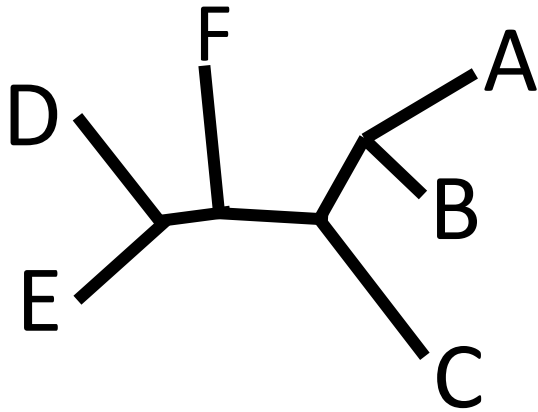
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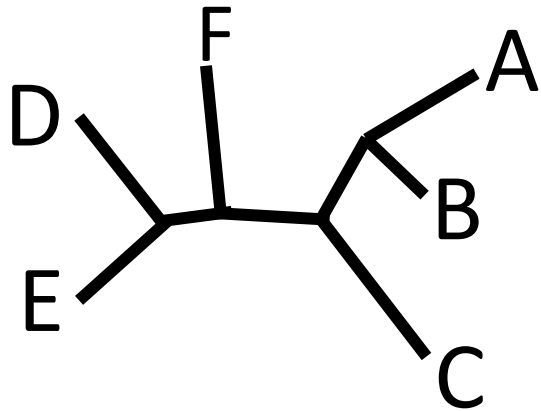
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# The root could be placed on any branch

E.g. an unrooted tree with 6 nodes

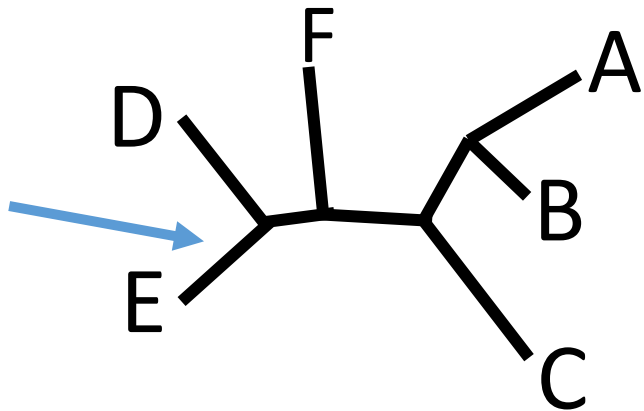


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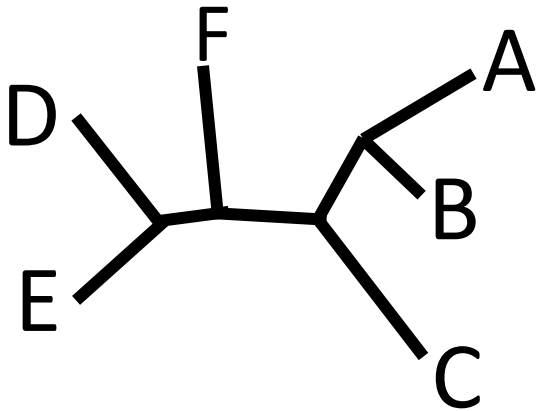
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# The root could be placed on any branch

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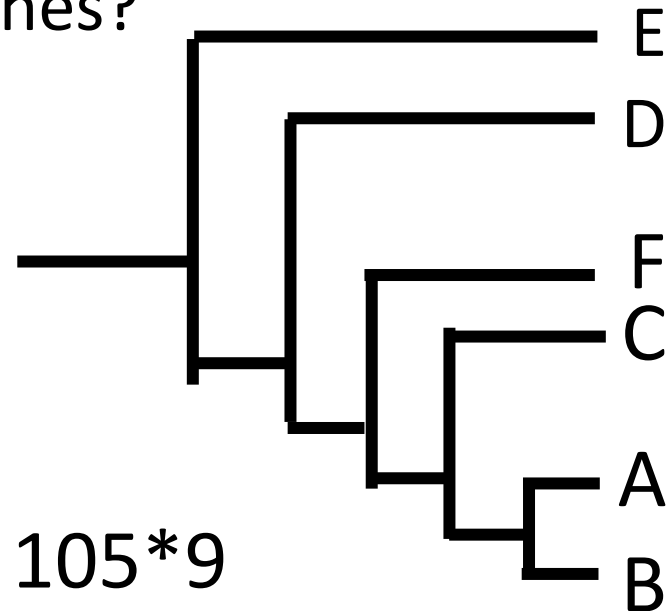
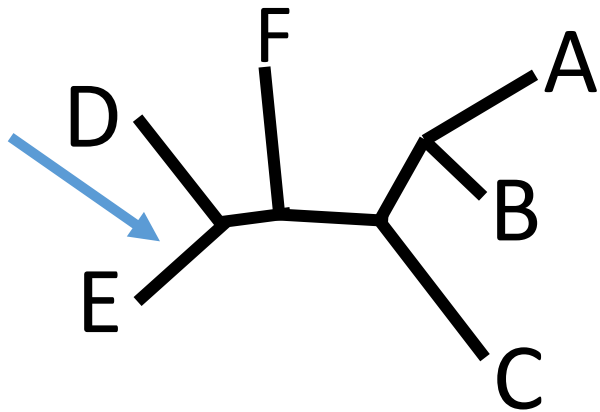


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How many branches?

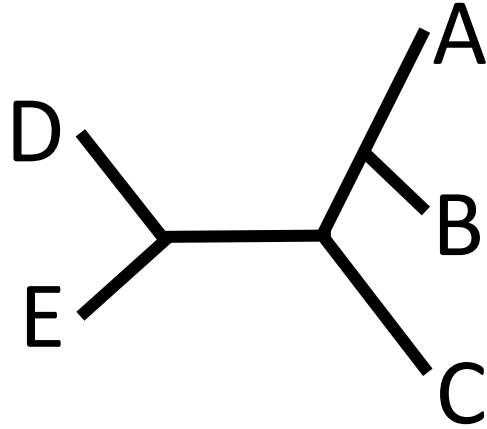
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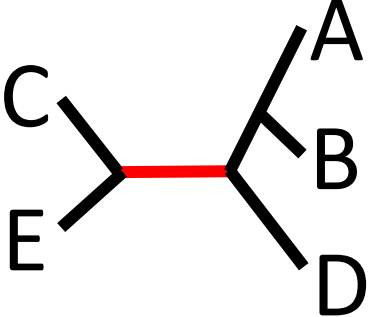
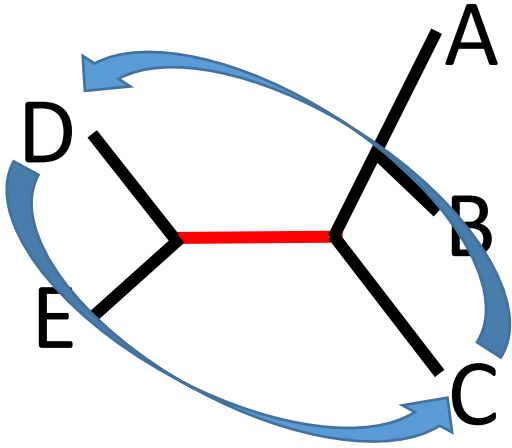
$$\begin{aligned} \text{Total options} &= 105 * 9 \\ &= \mathbf{945} \end{aligned}$$

# Nearest Neighbor Interchange trees

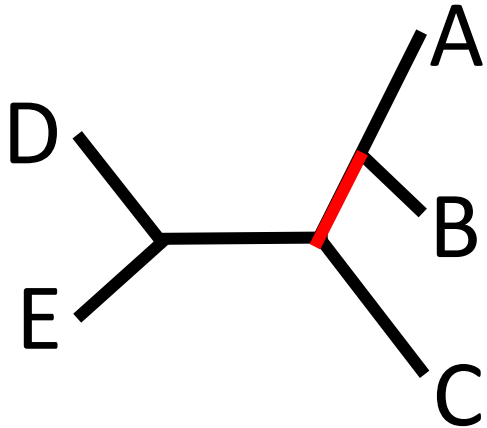
For each **internal branch**  
generate two variant trees  
that swap the  
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# Nearest Neighbor Interchange trees

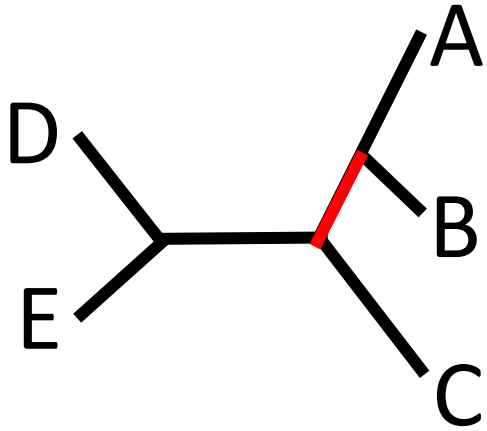
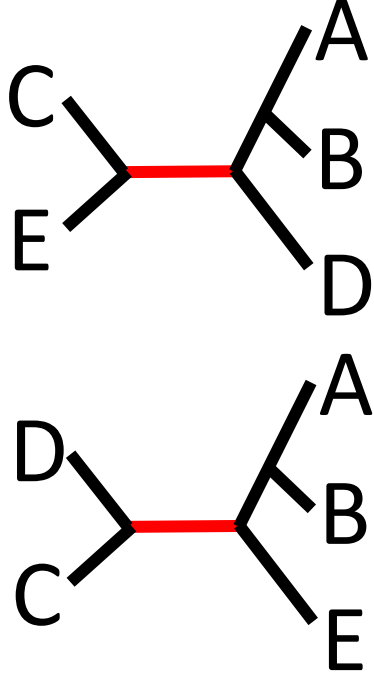
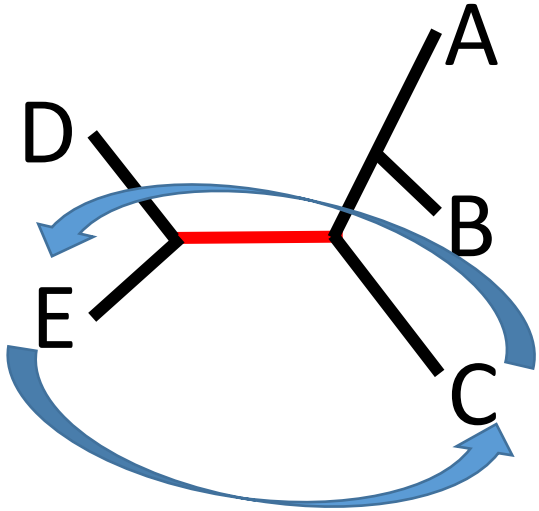


For each **internal branch** generate two variant trees that swap the relationships of the four outside branches



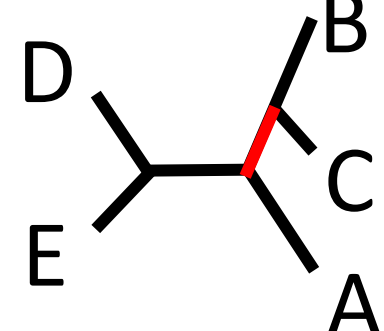
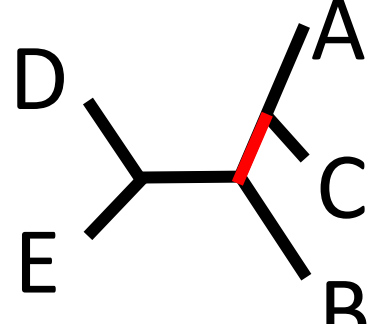
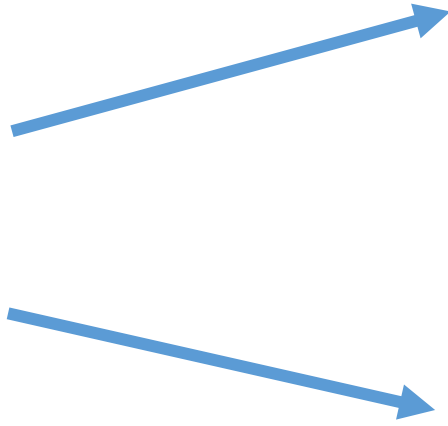
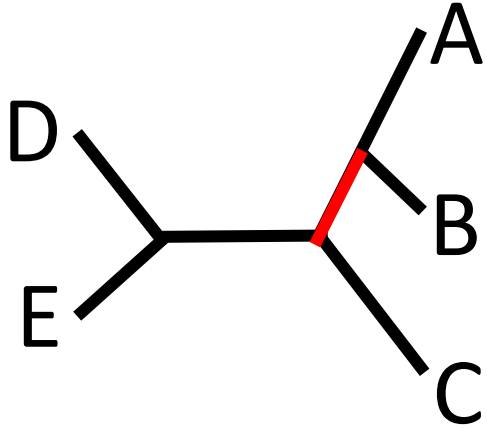
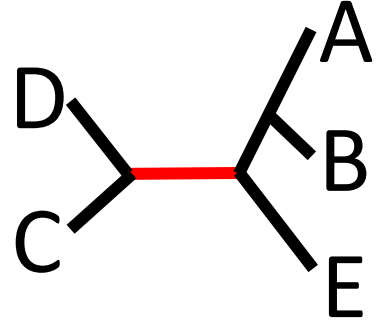
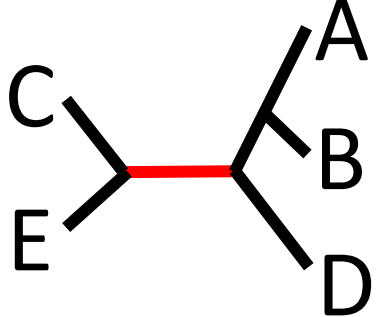
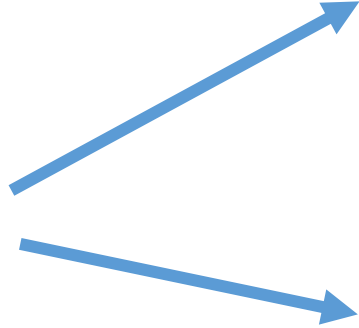
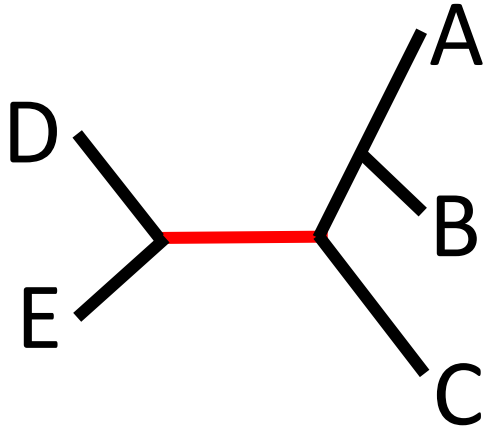
# Nearest Neighbor Interchange trees

For each **internal branch** generate two variant trees that swap the relationships of the four outside branches



# Nearest Neighbor Interchange trees

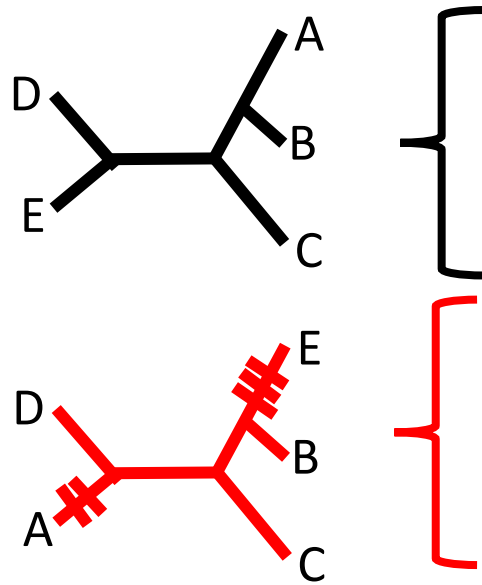
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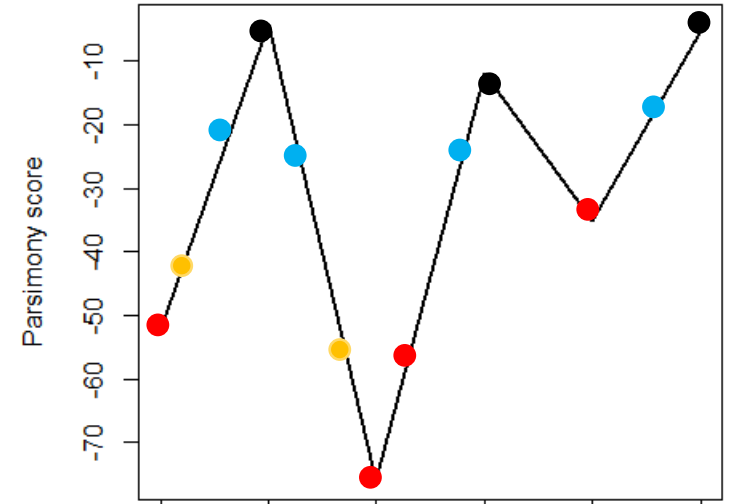
# Nearest Neighbor interchange keeps you from stepping too far in hill-climbing

Clades A and B are very closely related



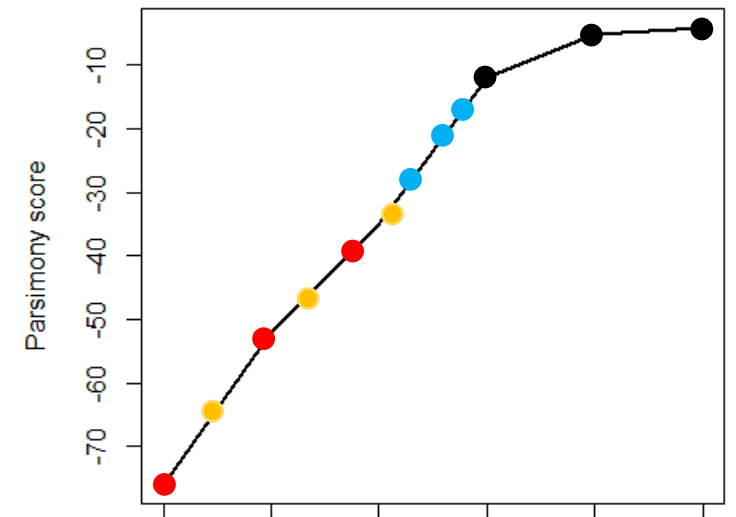
Tree	Negative parsimony Score
1	-12
2	-4
3	-5
4	-76
5	-52
6	-30

Random designation of neighbors

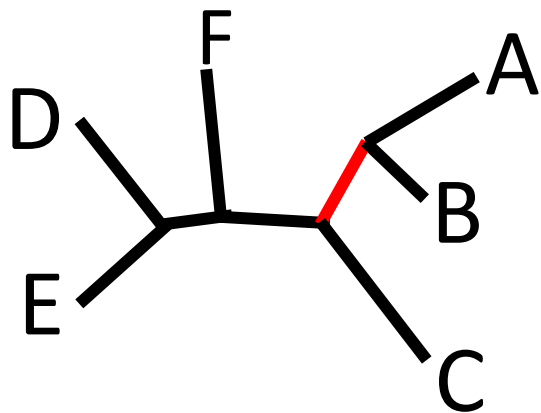


Tree position on surface

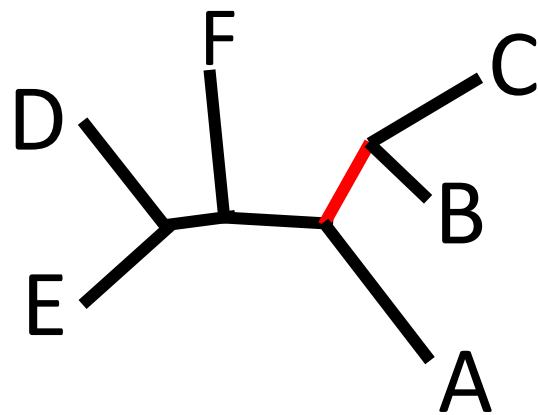
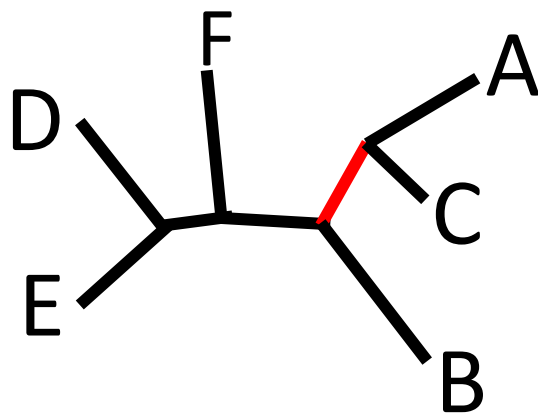
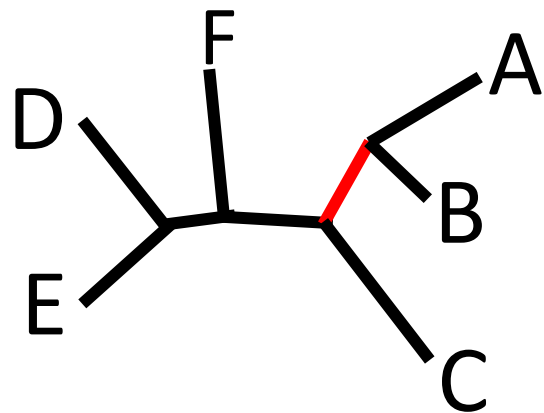
NNI designation



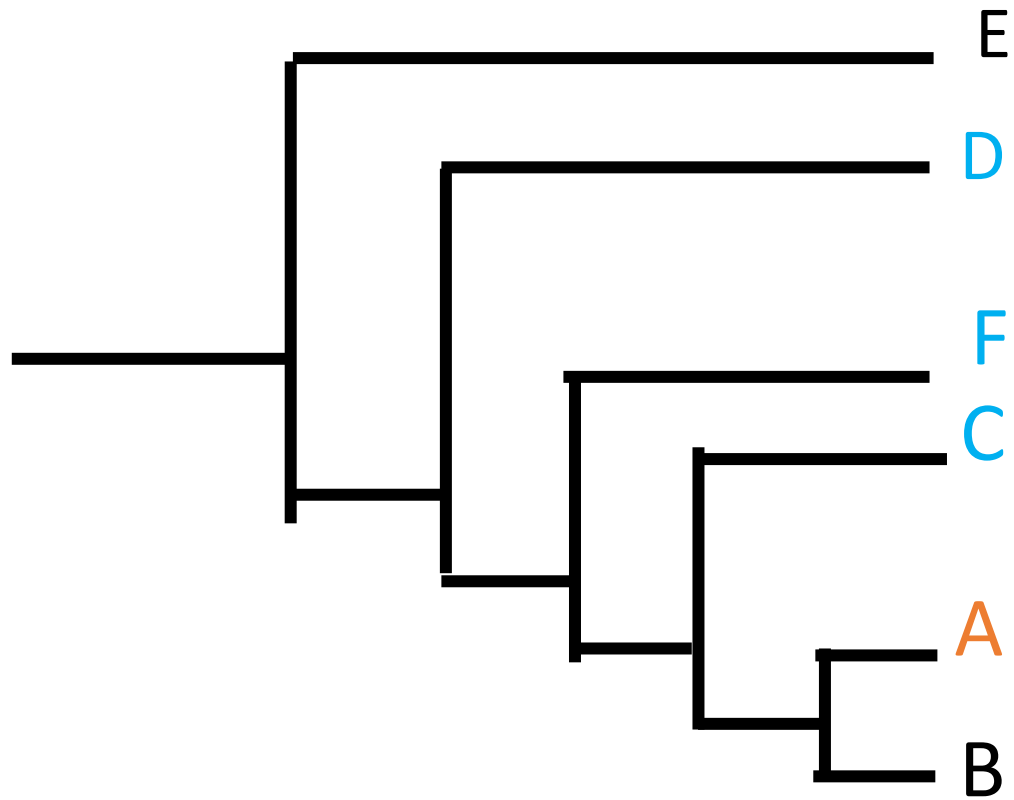
NN Practice: Draw both interchanges from swapping this branch



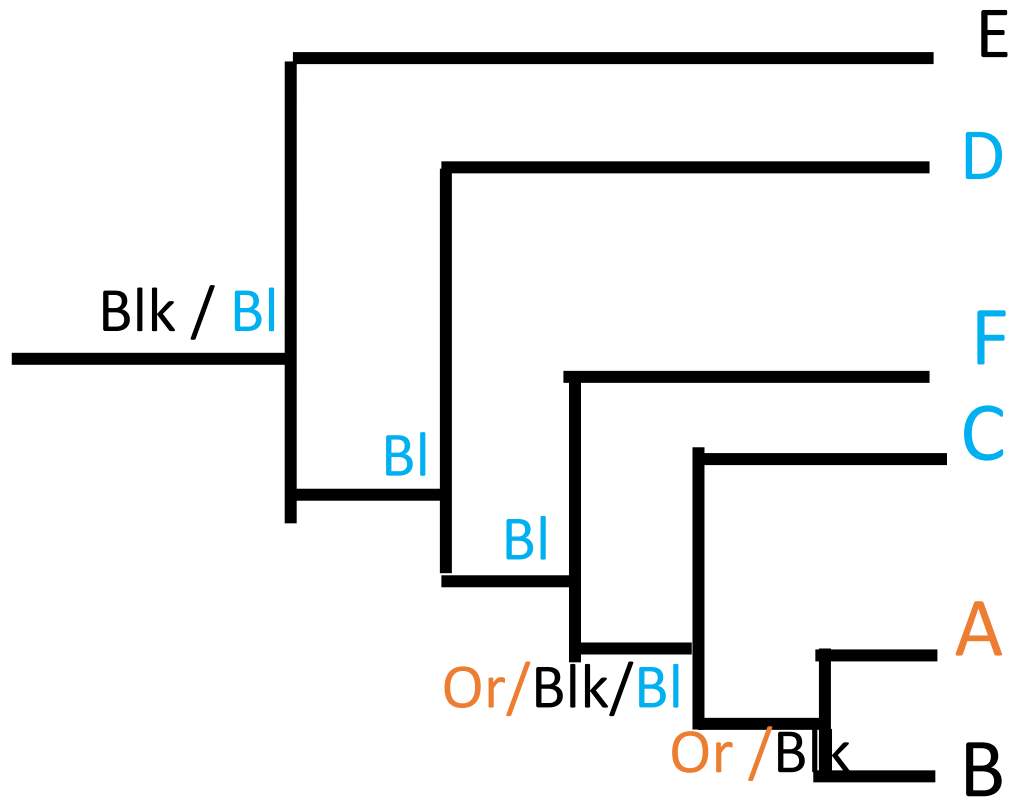
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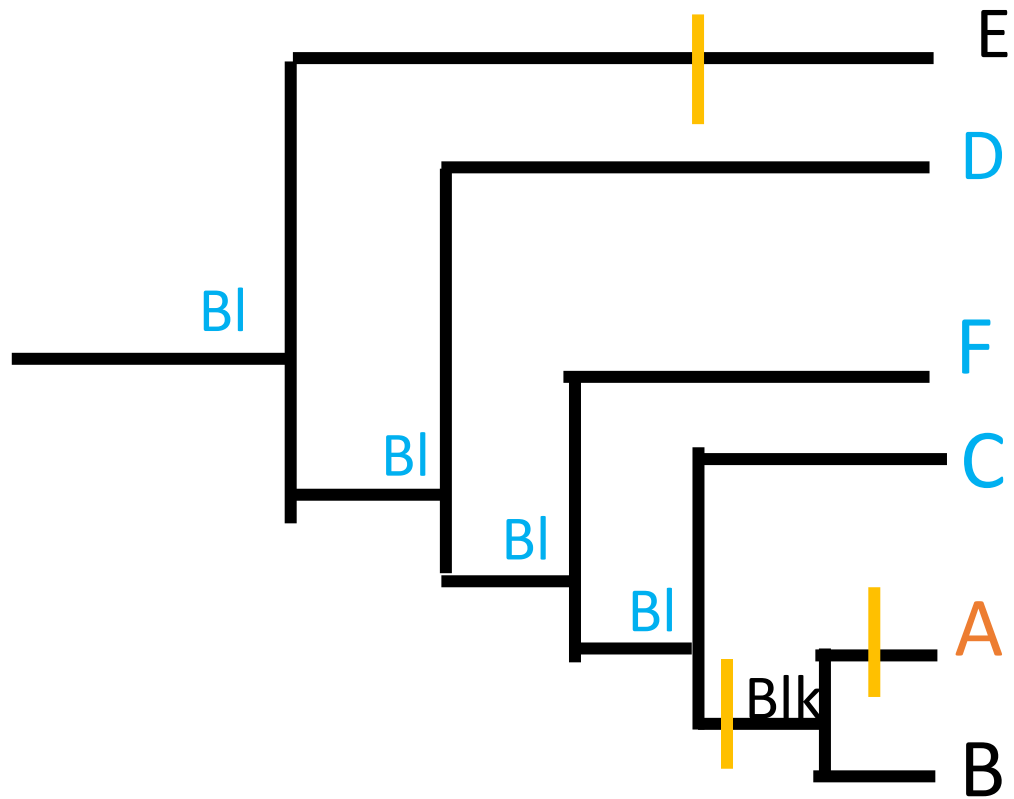
# Fitch algorithm practice



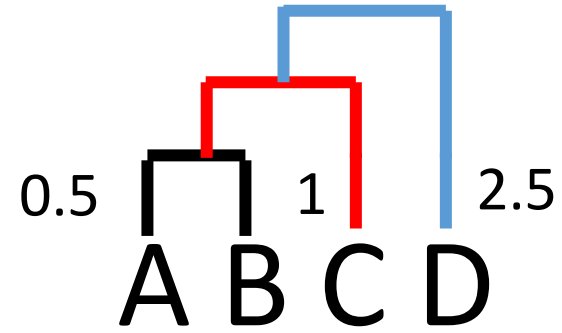
# Fitch algorithm practice: bottom-up



# Fitch algorithm practice: top-down



# Hierarchical clustering with complete linkage example



	A	B	C	D
A	0	1	2	4
B	1	0	2	5
C	2	2	0	5
D	4	5	5	0

	A,B	C	D
A,B	0	2	5
C	2	0	5
D	5	5	0

	A,B,C	D
A,B,C	0	5
D	5	0

# Programming note: 2D matrices in Python

- List of lists!
- Each row is a different list

	A	B	C	D
A	0	1	2	4
B	1	0	2	5
C	2	2	0	5
D	4	5	5	0

```
matrix = [ [0, 1, 2, 4], [1, 0, 2, 5], ...]  
print matrix[0][1]  
1  
print matrix[0]  
[0, 1, 2, 4]
```



Reminder: “Big O” notation for complexity

What is the time complexity in  $O()$  to compute the sum of a list?

```
# x is a list of length N
sum = 0
for v in x:
    sum = sum + v
print 'The sum is:', sum
```

Directly proportional to # of items in list!  $O(N)$

How about the time complexity in  $O()$  to compute the sum of an  $N \times N$  matrix?

```
# x is a list of N lists
# each list has N elements
sum = 0
for row in x: # Do this N times
    for v in row: # N times again
        sum = sum + v
print 'The sum is:', sum
# The answer is  $O(N^2)$ 
```

# Given a list of 2D points, compute their center

```
points = [ [1,2], [3,4], [5,6], [7,8] ]
# center point is ( mean_x, mean_y )
mean_x = 0.0
mean_y = 0.0
for i in range(0, len(points)) :
    mean_x += points[i][0]
    mean_y += points[i][1]

center = ( mean_x/len(points), mean_y/len(points) )
print center
(4.0, 5.0)
```

# Reading data from a file in Python

```
fin = open('qs5.txt', 'r') # 'r' stands for
'read'
all_lines = []
for line in fin: # In a for loop, fin acts
like a list of strings
    print line
    all_lines.append(line)
fin.close() # Lets the computer know it can
free up resources used to read the file
print all_lines
```

# Alternative file-reading structure

```
my_open_file = open(sys.argv[1])  
s1 = my_open_file.readline().strip()  
s2 = my_open_file.readline().strip()
```

Note: if in a different directory, have to supply **file path, e.g.:**  
python myScript.py /Users/cecilia/genome373/dataFile.txt

# Writing data to a file

```
fout = open('output.txt', 'w') # 'w'  
stands for 'write'  
fout.write('Hello! How')  
fout.write(' are you?\nI'm fine.') #  
'\n' starts a  
new line  
fout.close()
```

# Useful function: Split a string into its constituent words

```
s = 'Wherefore art thou Romeo?'  
words = s.split() # Returns a list of substrings  
print words
```

```
['Wherefore', 'art', 'thou', 'Romeo?']
```

```
# split() can use any arbitrary string to split by
```

```
words = s.split('r')
```

```
print words
```

```
['Whe', 'efo', 'e a', 't thou Romeo?']
```